

# Trigonometric Delights

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Eli Maor

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**I**n memory of my uncles

*Ernst C. Stiefel (1907–1997)*

*Rudy C. Stiefel (1917–1989)*

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